

**Advanced Methods for ODE and DAE:**  
*Assignment 3*

**Exercise 1:** *due date: 17.5.* **(10 points)**

Set up the general spring mass model with  $N$  masses, analogously to Keplers problem, as first-order system. Prove that its solutions are stable in the sense of Lyapunov, you can proceed as in tutorial (using Hamiltonian). A little pdf is on studip to simplify the start for you.

**Exercise 2:** *due date: 10.5.* **(36 points)**

(a) Implement a general ( $A, b, c$  are parameters) implicit RK method, using a Newton solver, in python, using  $A, b, c$  of a method of order  $p$ . The points are for design. (8 points)

(b) Apply it to  $\dot{x} = \lambda x$ ,  $\lambda < 0$ . The points are for code working for 1D problem. (8 points)

(c) Apply it to a 2-spring 2-mass problem. The points are for code working for 4D problem and problem itself. (12 points)

(d) *due date: 17.5.* Make convergence plots for comparing two methods of different order of your choice, using one of the above problems or one of your interest. (8 points)  
Do not forget plots.